

Modelling the Collections Policy

Christophe Mues Mee Chi So Lyn Thomas
University of Southampton

Adiel T. De Almeida Filho
Federal University of Pernambuco

Debt Collections

- A multi-billion dollar industry:
 - £12 billion of loans to corporate and individuals were being written off by UK financial institutions in 2012 (Bank of England, 2013)
- Actions: formal letters, persistent phone calls, legal procedures, etc. (Coleman, 2004)
- No return on actions: ordered in terms of their perceived harshness
- Many problem aspects to consider: How long? In what sequence? Who should be contacted first?

Outline of the Talk

- Current practice and related literature
- Dynamic programming model
- Numeric example; results
- Conclusions and possible extensions

Current Practice & Related Literature

- Using **collection scorecards** (e.g. Experian, 2006)
- Score could reflect how likely is a defaulter to pay back a “satisfactory” percentage of the defaulted debt
- Segment the defaulted population based (in part) on score band they are in
- Different actions for different segments
- Choice of strategy may be based on expert judgement, experimentation, mathematical optimisation (e.g. also taking into account resource constraints)
- Little if any work reported in the academic literature though

Related Literature: LGD

- Growing number of papers on estimating **Loss-Given-Default (LGD)** or **Recovery Rate (RR)**
- Only a few of them look at the interaction between policy and LGD, e.g.:
 - Matuszyk et al. (2010): when and whether to recover “in house” for consumer loan
 - De Almeida Filho et al. (2010): at portfolio level
 - Weber (2012): self-exciting point process
 - Probability of paying back some percentage of balance
 - Stochastic intensity of repayment arrival times allowed to depend on actions of the lender
 - Han and Jang (2013): corporate credit and whether the lender's actions can impact LGD

Bayesian Dynamic Programming

- In this paper, we present current work on using **Bayesian dynamic programming** to optimise the collections strategy at the individual loan level
- Approach introduced to credit granting models by Bierman and Hausman (1970)
- Uncertainty about a parameter value (here: repayment probability, assumed to be a Bernoulli random variable) is described by a Beta distribution
 - Allows us to work at the individual defaulter level and take into account previous payment performance of that defaulter; i.e., the collector's belief about the repayment probability is updated at the end of each time period (e.g. calendar month)

Proposed Collections Model and Notation

- Performance history (by defaulter)
 - i : the current action
 - s : no. of periods under action i
 - m : no. of repayments under action i
 - r : the RR when the collector started using action i
- $V(r, s, m, i)$: the future net discounted RR
- At the beginning of each time period, two possible decisions for the lender:
 - Stay in action i
 - Move to action $i + 1$
- How to choose the optimal decision (i.e. the one that maximises the resulting RR)?

Move to Action $i + 1$

- $V(r, s, m, i) \rightarrow V(., 0, 0, i + 1)$
- Define
 - $f_i(m)$ to be the RR of the m^{th} repayment under action i (i.e., pct. of debt outstanding at start of using action i that is repaid in the m^{th} actual repayment under action i)
 - $F_i(m) = \sum_{j=1}^m f_i(m)$ to be the cumulative RR in the m^{th} repayment under action i
- Therefore, if the lender moves to action $i + 1$, the future net discounted RR will be:

$$V(r + (1 - r)F_i(m), 0, 0, i + 1)$$

Stay in Action i

- What is the expected recovery rate from this point onward?
 - *Repayment*: $(1 - r)f_i(m + 1) + \beta V(r, s + 1, m + 1, i)$
 - *No repayment*: $0 + \beta V(r, s + 1, m, i)$
- Repayment probability $B(s, m)$; expected value: m/s
- For action i , introduce prior of the repayment probability $B(s_0^i, m_0^i)$
- Hence, if the lender keeps in action i , the future net discounted RR will be:

$$\frac{(m + m_0^i)}{(s + s_0^i)} \text{Repayment} + \left(1 - \frac{(m + m_0^i)}{(s + s_0^i)}\right) \text{No repayment} - c_i$$

The Model and Some Optimality Results

- Therefore, the Bayesian dynamic program model is:

$$V(r, s, m, i) = \max \begin{cases} \frac{(m + m_0^i)}{(s + s_0^i)} [(1 - r)f_i(m + 1) + \beta V(r, s + 1, m + 1, i)] + \left(1 - \frac{(m + m_0^i)}{(s + s_0^i)}\right) [0 + \beta V(r, s + 1, m, i)] - c_i & (1) \\ V(r + (1 - r)F_i(m), 0, 0, i + 1) & (2) \end{cases}$$

$$P(r, s, m, i) = \begin{cases} 1, & \text{if (1) is chosen} \\ 2, & \text{otherwise} \end{cases}$$

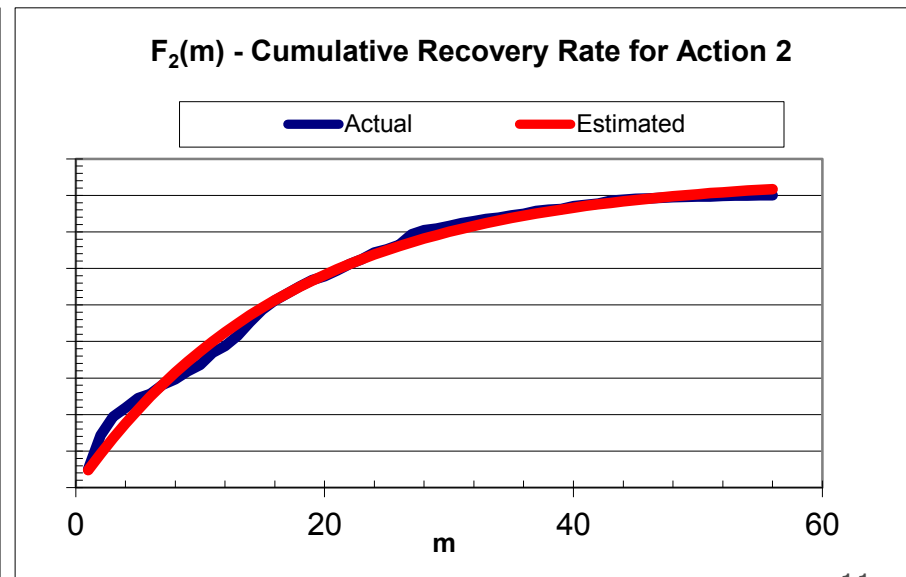
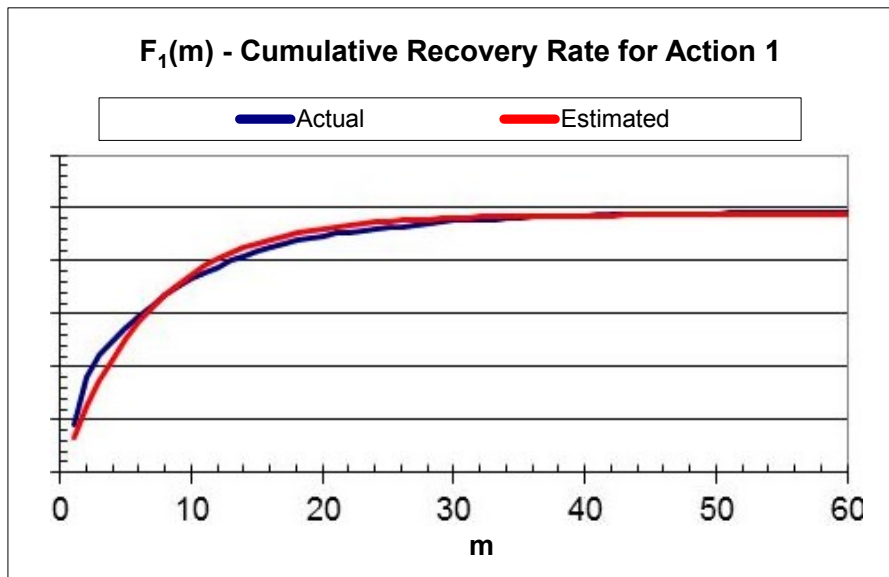
- Solving the model with value iteration (Puterman, 2005)
- Some optimality results:
 - One keeps on with action i if $s < s^*(r, m, i)$; One moves to action $i+1$ if $s \geq s^*(r, m, i)$.
 - If RR is a constant under action i , i.e. $f_i(m) = f_i$, then $s^*(r, m, i) \leq s^*(r, m + 1, i)$

A Numeric Example

- Collection data from a European bank
- 3,000+ defaulted consumer unsecured loans
- Using data, exponential function fits well with $f_i(m)$

Therefore, we define:

$$f_i(m) = a_i e^{-b_i m}. \text{ Hence } F_i(m) = \sum_{j=1}^{j=m} f_i(j) = \frac{a_i(1-e^{-b_i m})}{(1-e^{-b_i})}$$

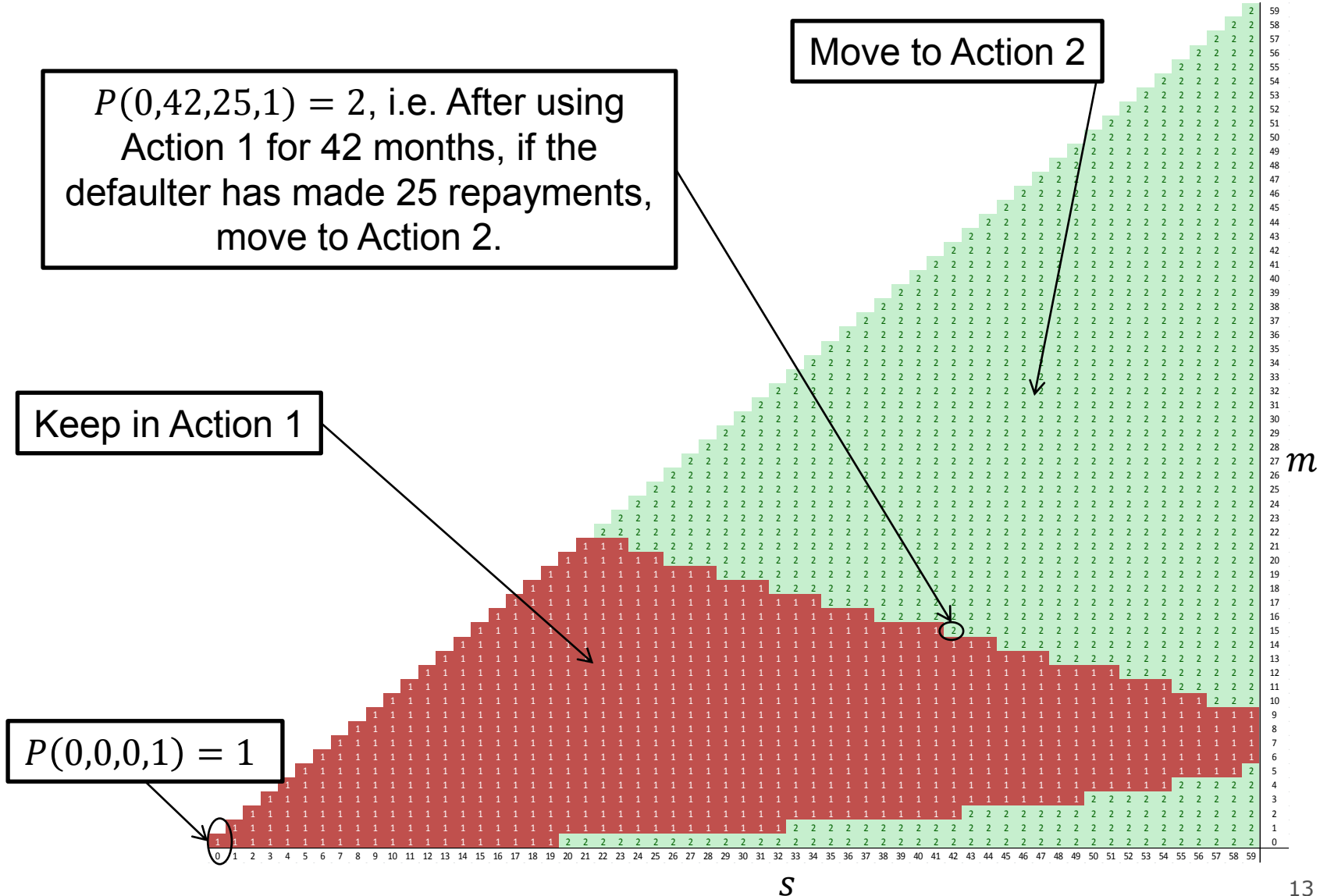


A Numeric Example: Parameters

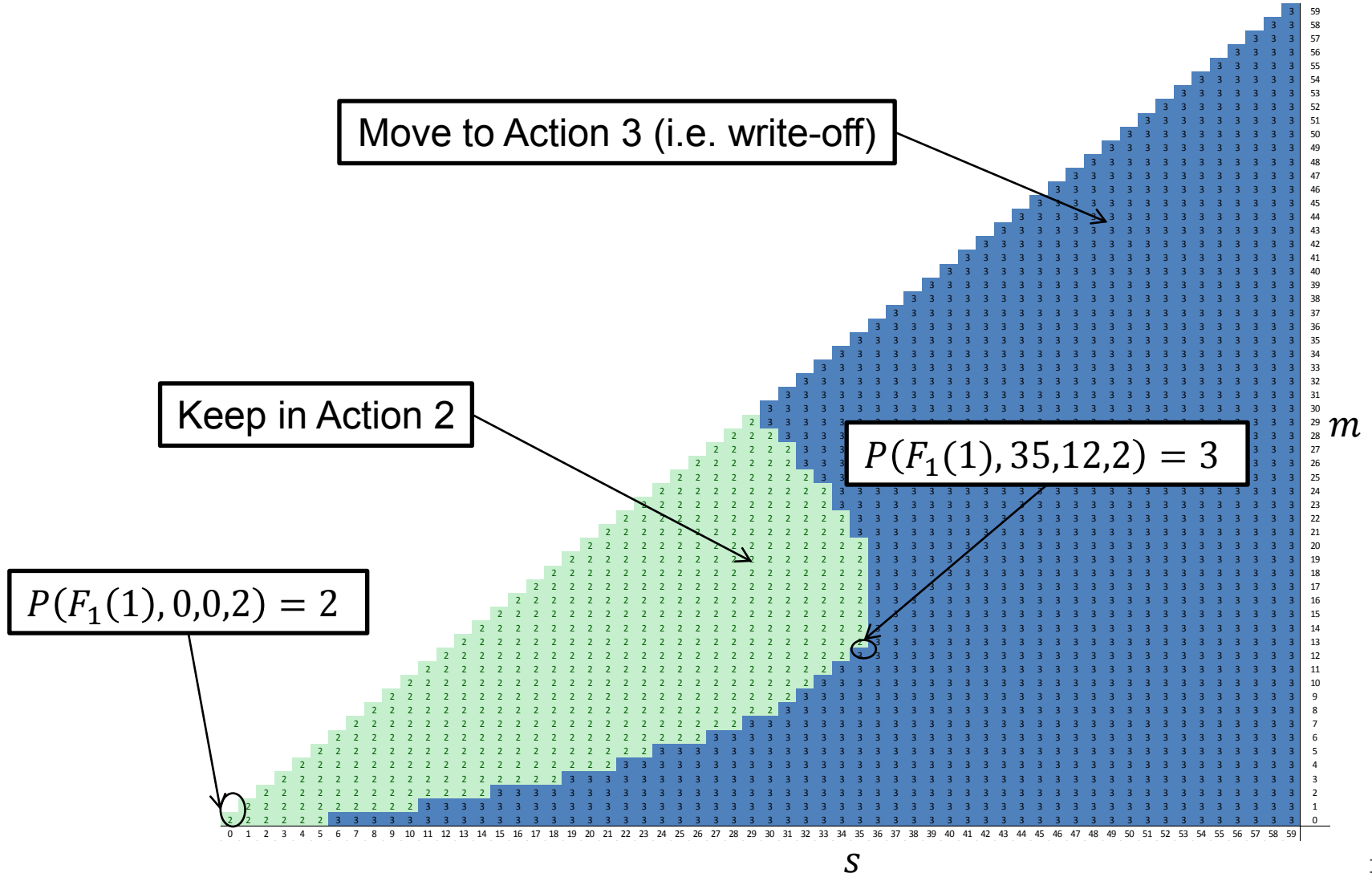
Actions	a_i	b_i	Monthly Cost (c_i)	s_0^i	m_0^i
1 – General communication	0.035721	0.1470	0.00048656	2	1
2 – Legal procedure	0.024522	0.0577	0.00398703	2	1
3 – Write-off (The boundary condition)	-	-	0	-	-

- Solving the model with value iteration
- Maximum $m = 60$ (5 years)
- Find the optimal policy for different (r, s, m, i)

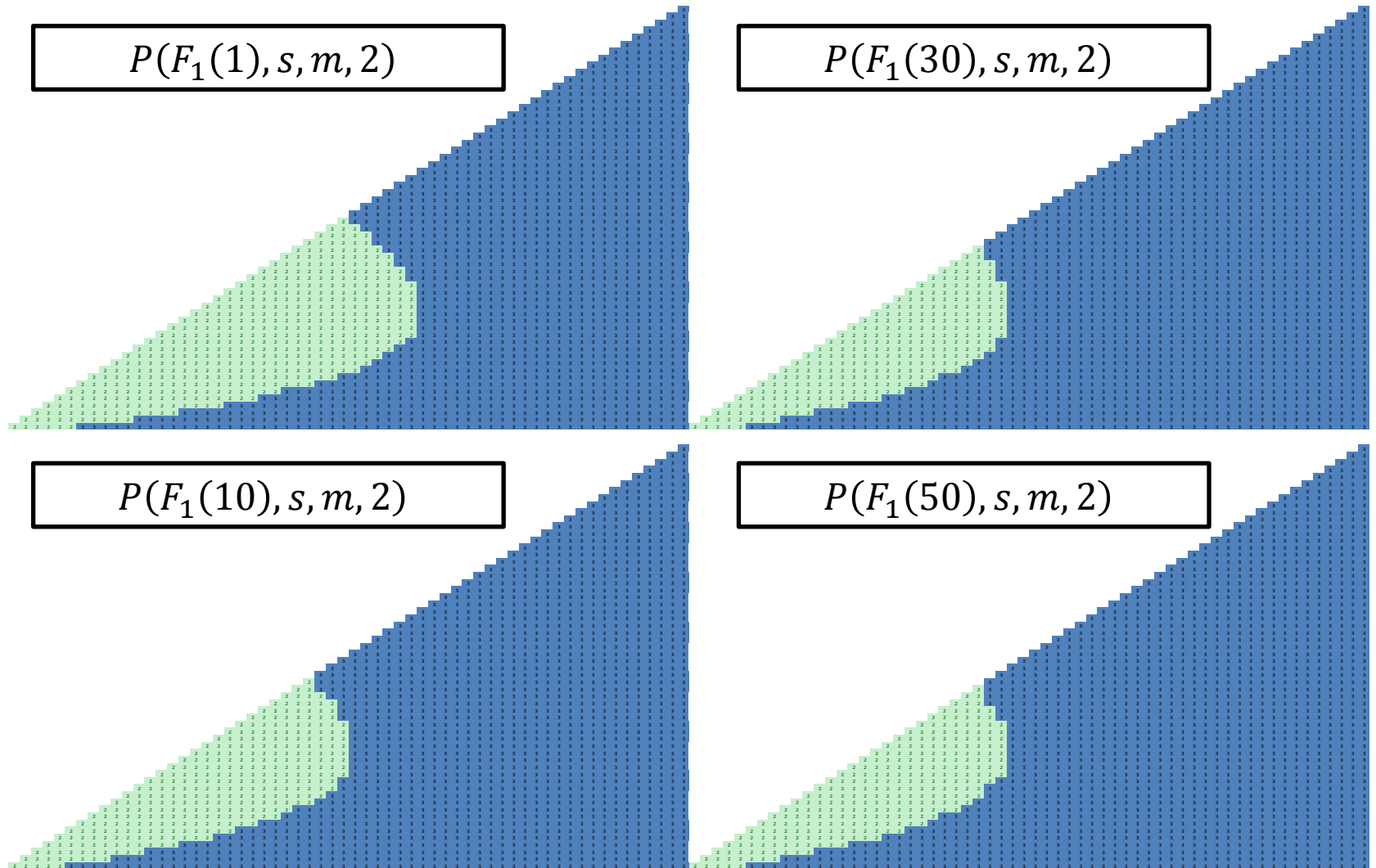
Optimal Policies for $(0, s, m, 1)$



Optimal Policies for $(F_1(1), s, m, 2)$



Optimal Policies for $(F_1(\cdot), s, m, 2)$

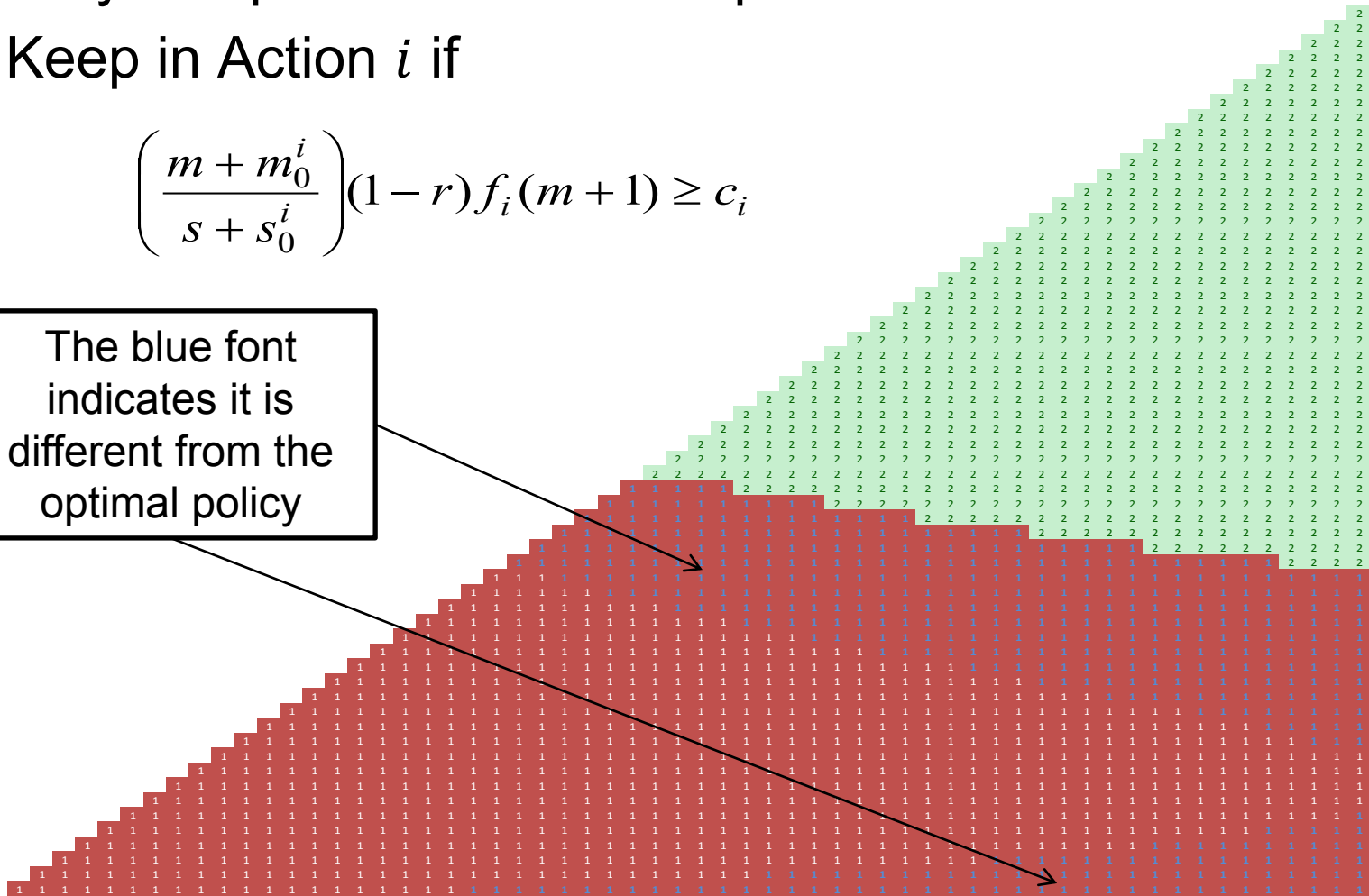


Myopic Policies for $(0, s, m, 1)$

- Only compare the current expected RR vs. the cost
- Keep in Action i if

$$\left(\frac{m + m_0^i}{s + s_0^i} \right) (1 - r) f_i(m + 1) \geq c_i$$

The blue font indicates it is different from the optimal policy



Myopic Policies for $(F_1(\cdot), s, m, 2)$

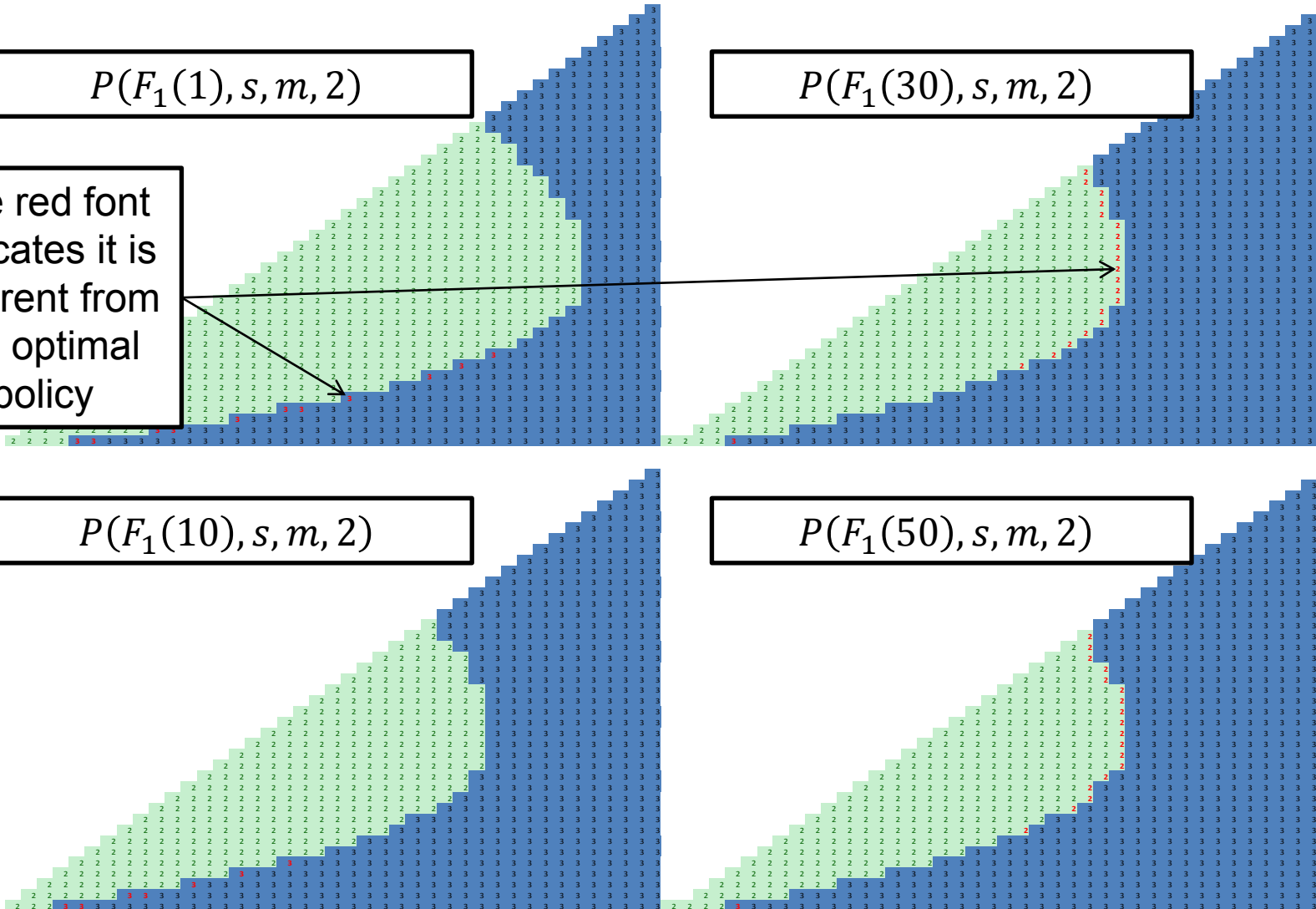
$P(F_1(1), s, m, 2)$

The red font indicates it is different from the optimal policy

$P(F_1(30), s, m, 2)$

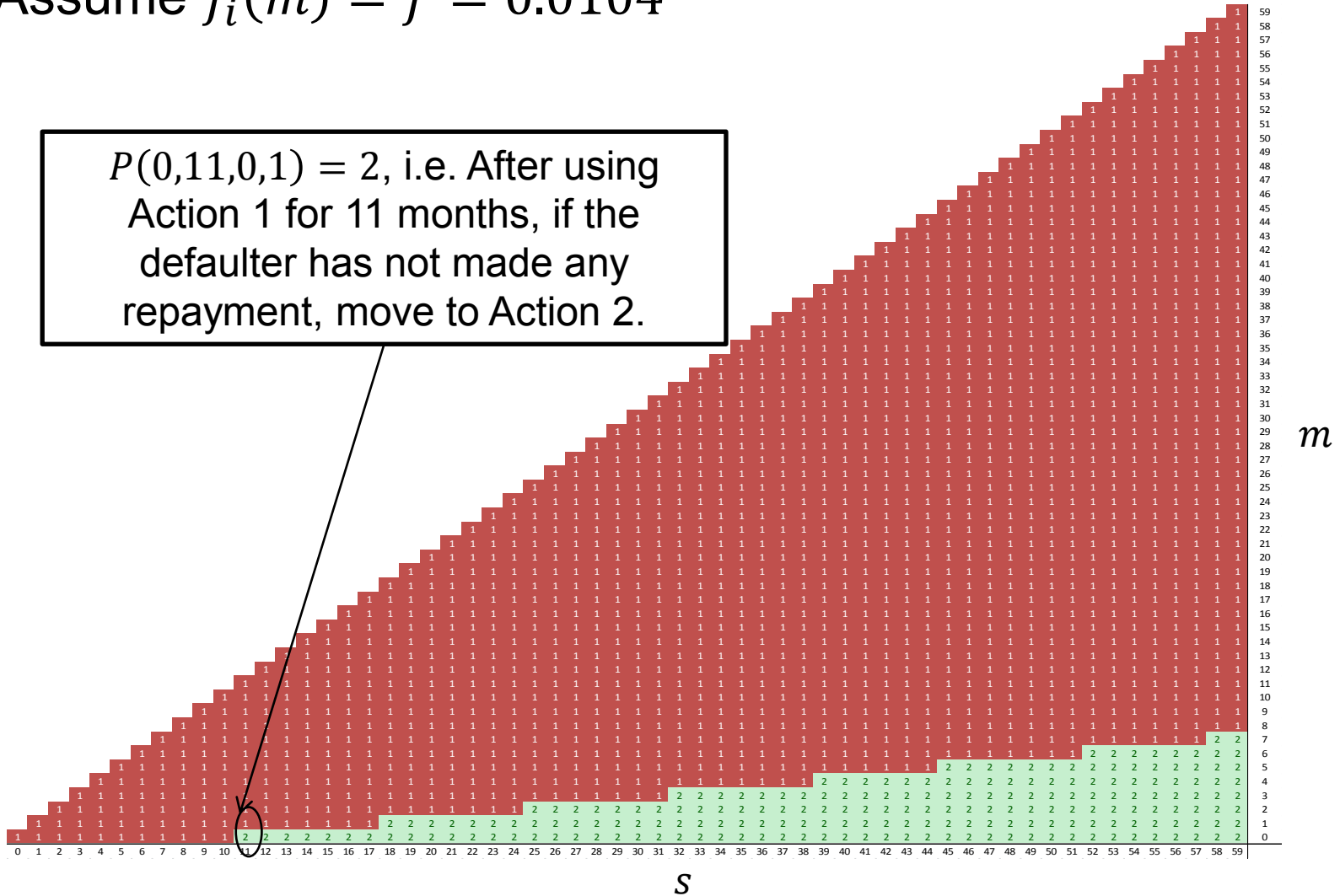
$P(F_1(10), s, m, 2)$

$P(F_1(50), s, m, 2)$



A Fixed Repayment Amount for $(0, s, m, 1)$

- Assume $f_i(m) = f = 0.0104$



A Fixed Repayment Amount for $(F_1(\cdot), s, m, 2)$

$$P(F_1(1), s, m, 2)$$

$$P(F_1(30), s, m, 2)$$

$$P(F_1(10), s, m, 2)$$

$$P(F_1(50), s, m, 2)$$

Conclusions & Possible Extensions

- We argued the case for developing policies that:
 - Are based on performance of individual customer
 - Reassess course of action at end of each time period
 - Take into account there is usually a sequence of actions to consider and one needs to “look ahead”
- Flexible approach: possible extensions
 - Could include a fixed cost for starting a new action
 - The RR can be made a function of s as well: $F(m, s)$
 - Prior could use any available loan- or debtor-specific information (thus extending the idea of a collection score) or even a function of the economic conditions (estimate recovery rate or LGD in downturn conditions)

List of References

- Coleman, A. M. 2004. *Collection Management Handbook*, John Wiley, Hoboken.
- De Almeida Filho, A. T., C. Mues, L. C. Thomas. 2010. Optimizing the Collections Process in Consumer Credit. *Production and Operations Management*. 19 698-708.
- Experian. 2006. The value of implementing scoring in the collection process. *Experian White Paper*, Almondsbury Bristol.
- Han, C., Y. Jang. 2013. Effects of debt collection practices on loss given default. *Journal of Banking and Finance*. 37 21-31.
- Matuszyk, A., C. Mues, L. C. Thomas. 2010. Modelling LGD for unsecured personal loans: decision tree approach. *Journal of Operational Research Society*. 61 393-398.
- Weber, T. 2012. Dynamic valuation of delinquent credit card accounts, EPFL-CDM-MTEI, *Ecole Polytechnique Federale de Lausanne*

Thank you

We welcome any comments or suggestions.